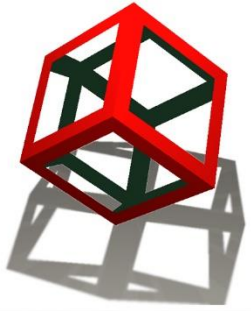


# Prediction of appearance of materials

The radiometric approach



GDR  
2044  
cnrs

APPAMAT

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French research group whose vocation is to organize and develop the scientific community around the appearance of materials

Axe 1 – Materials and fabrication

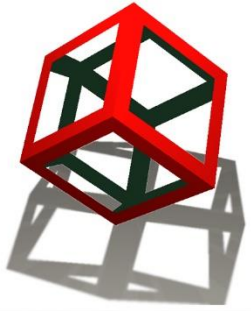
Axe 2 – Physical and sensory measurements

Axe 3 – Modeling and simulation

Axe 4 – Scanning and description

Axe 5 – Digital reproduction and rendering

<http://gdr-appamat.cnrs.fr>



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# Material Appearance Workshop

in partnership with CIC27

Organized by GDR APPAMAT   
21 October 2019, 9:00 – 18:00

Centre International de Conférences Sorbonne Universités  
(CICSU)

<http://gdr-appamat.cnrs.fr>

**Shape, Texture, Translucency, Gloss, Color  
are attributes of appearance**



Appearance  
attributes



**Appearance**  
Color, gloss, translucency

Radiometry



**Radiometric response**  
Spectral, angular and spatial distribution of  
reflected and transmitted light in the visible range

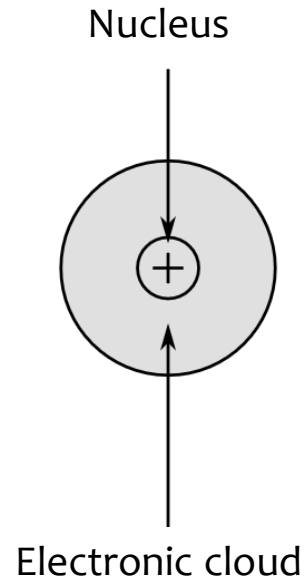
Electromagnetism



**Intrinsic optical properties  
of the components**  
Complex refractive index

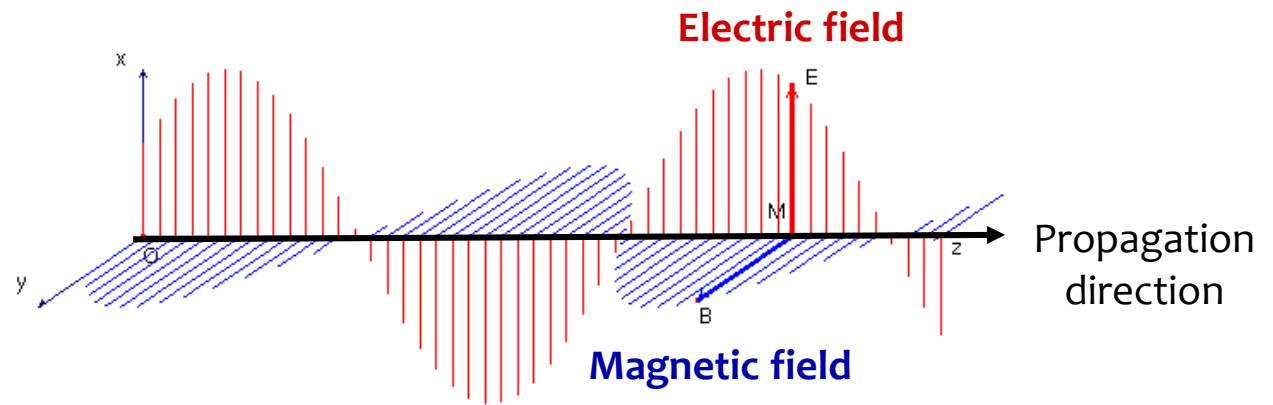
## Matter

Set of electrical charges

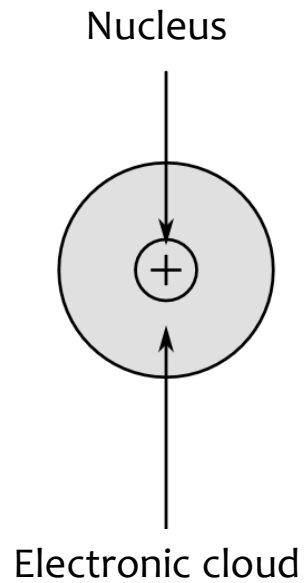


## Light

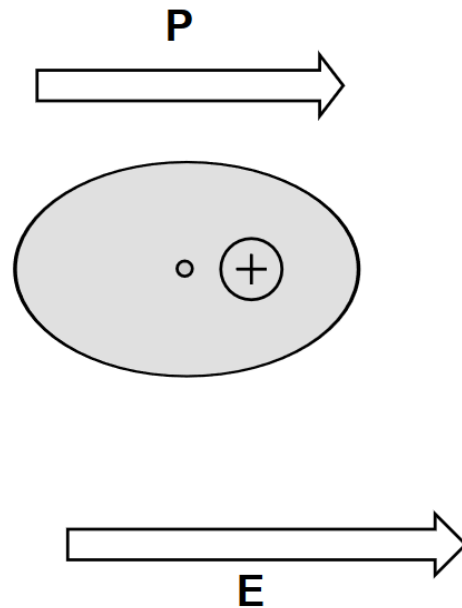
Electromagnetic wave



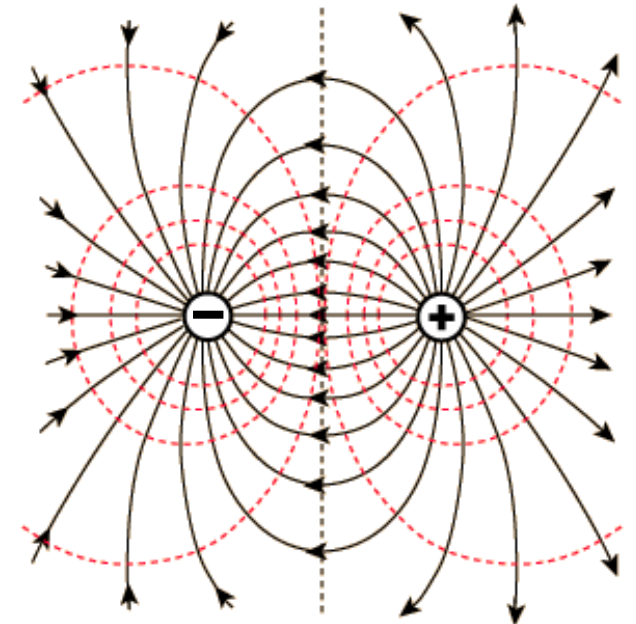
The **polarization direction** is the direction of the electric field **E** (perpendicular to the direction of propagation).



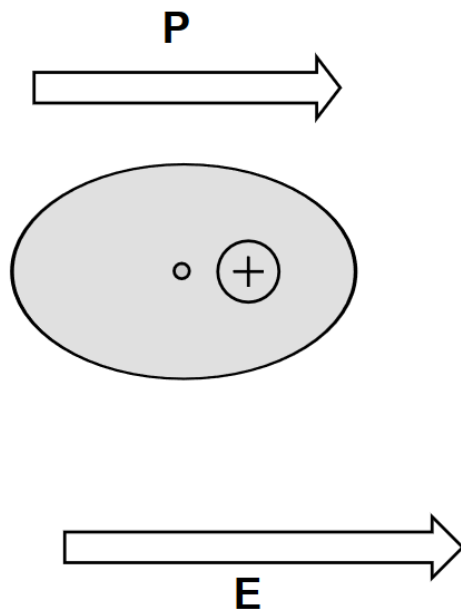
Subjected to an electric field  $E$  (i.e. light wave), matter becomes polarized



As a first approximation, it behaves like an electric dipole



The polarization vector  $\mathbf{P}$  corresponds to a dipole moment per unit volume



**Linearity assumption**

$$\mathbf{P} = (\epsilon - \epsilon_0) \mathbf{E}$$

$\epsilon$ : dielectric permittivity

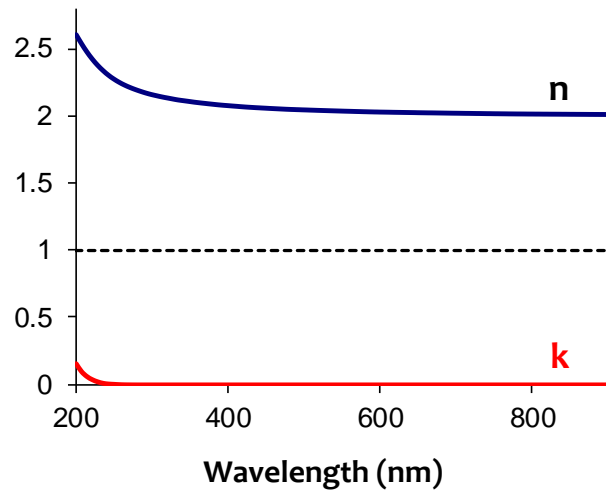
In optics, we prefer to use the **complex refractive index**

$$\underbrace{\mathbf{n}}_{\text{Refractive index}} + i \underbrace{\mathbf{k}}_{\text{Extinction coefficient}} = \sqrt{\frac{\epsilon}{\epsilon_0}}$$



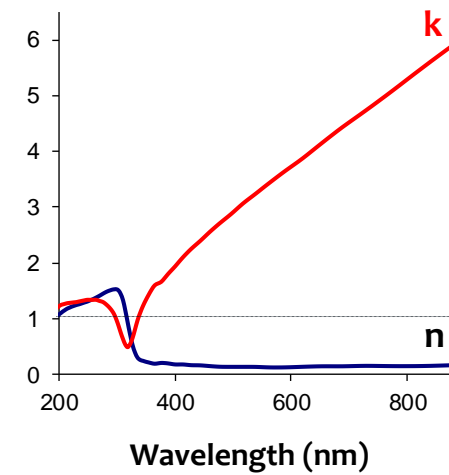
Complex refractive indices can be measured by ellipsometry or are tabulated

## Dielectrics

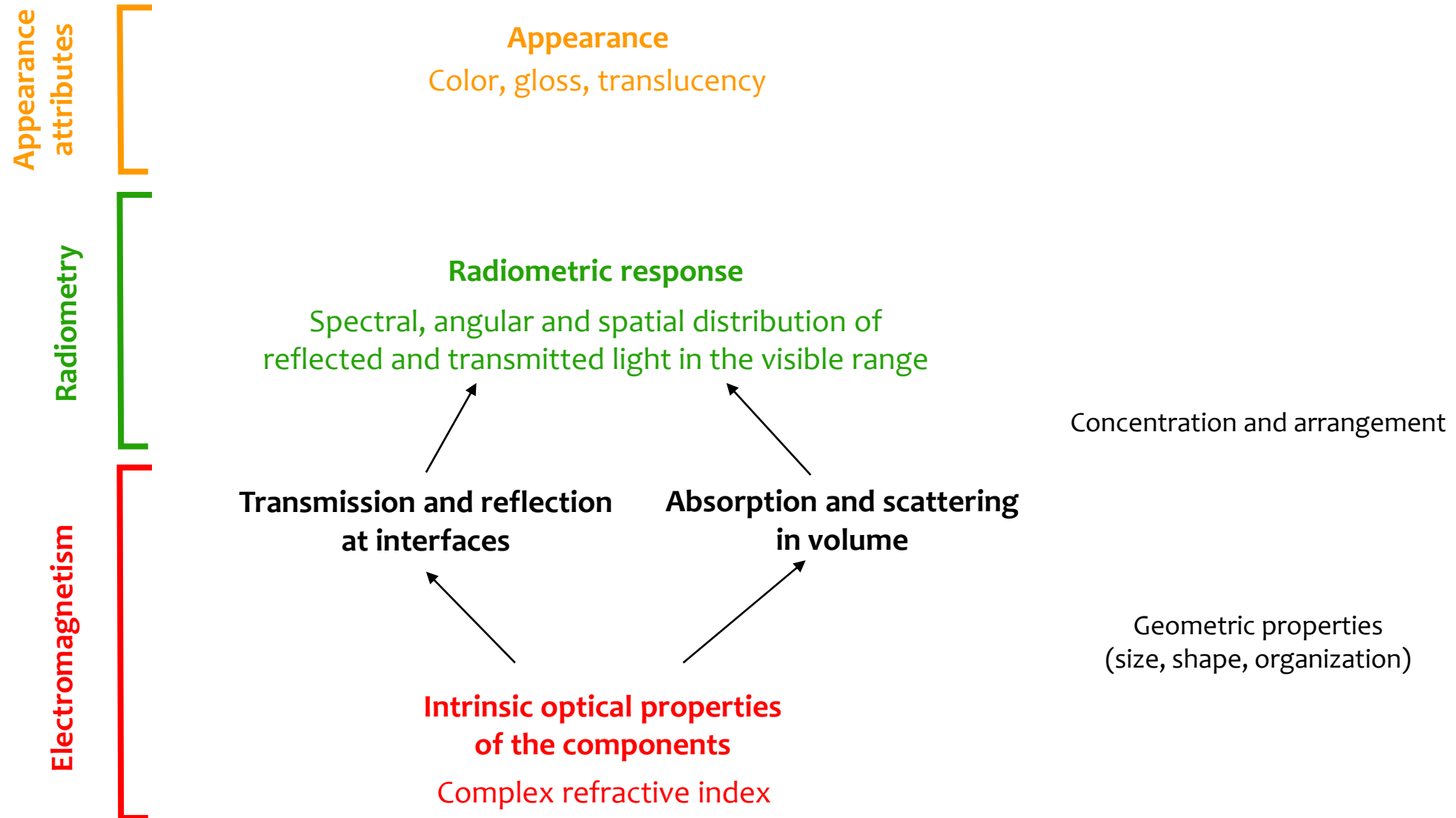


$\text{Si}_3\text{N}_4$

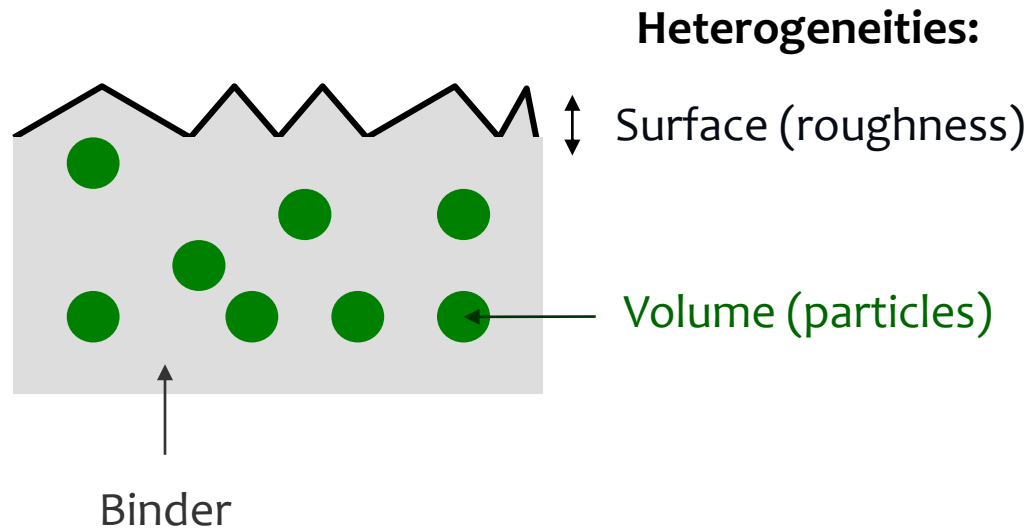
## Metals



Ag

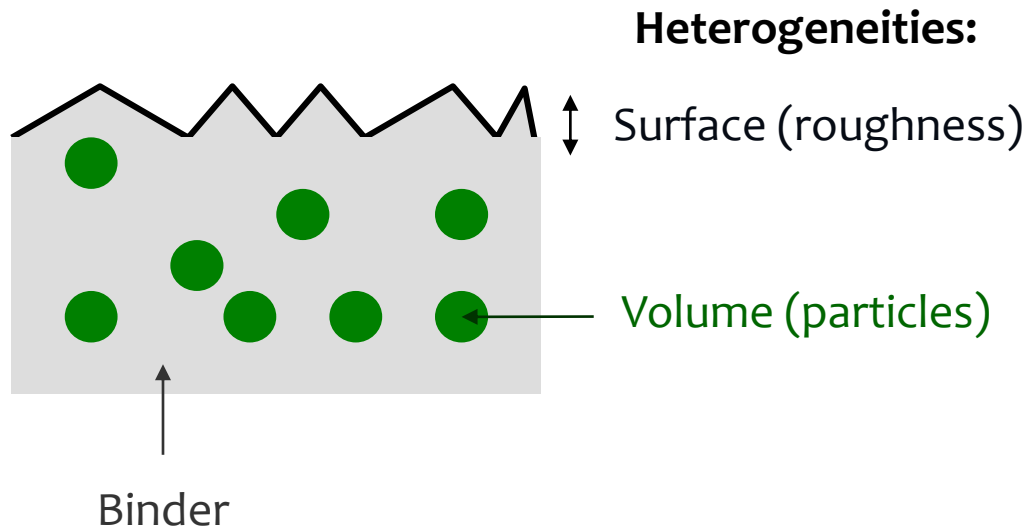


## Coating (paint, ink...) of a material

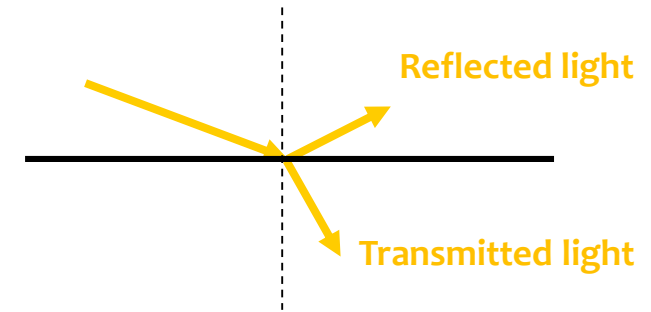


## Coating (paint, ink...) of a material

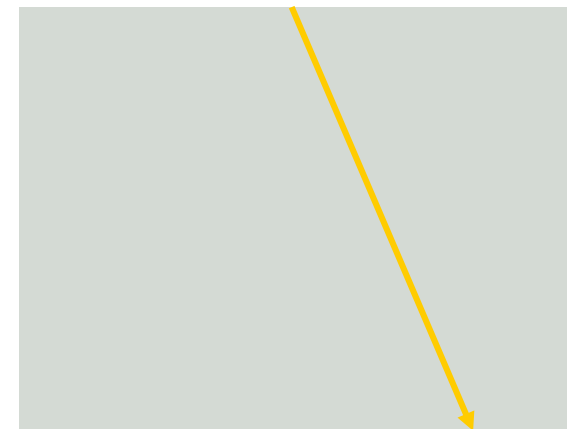
Low size and/or concentration



**"Effective" flat interface**  
(Snell-Descartes law, Fresnel relationships)

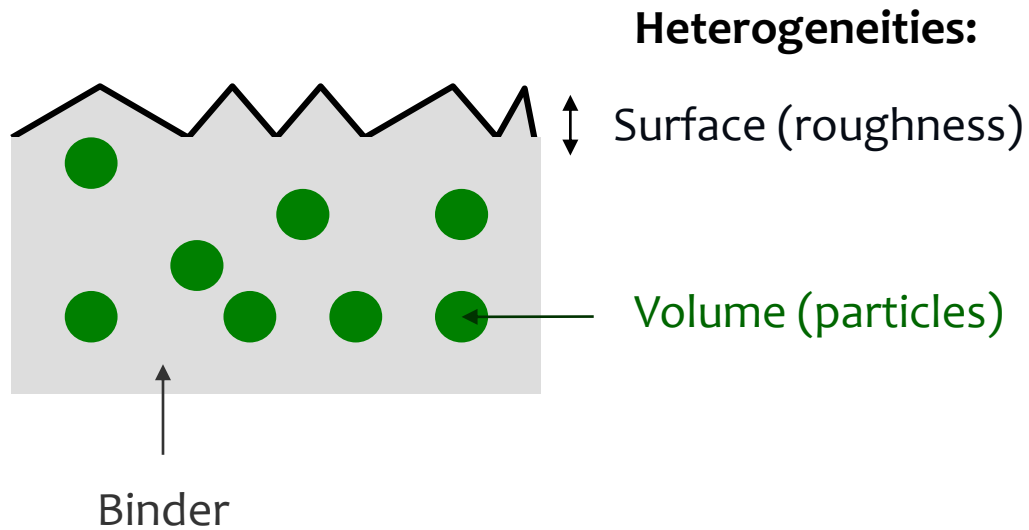


**Homogeneous "effective" medium**  
(straight propagation, Beer-Lambert-Bouguer law)

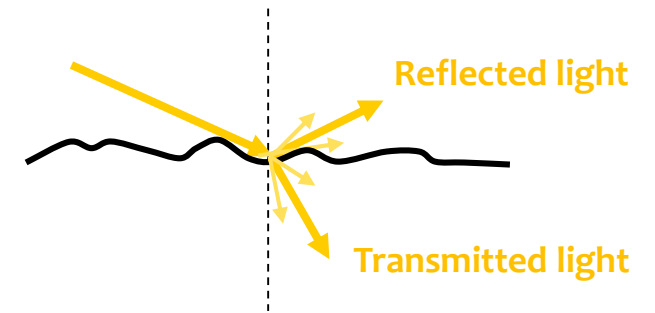


## Coating (paint, ink...) of a material

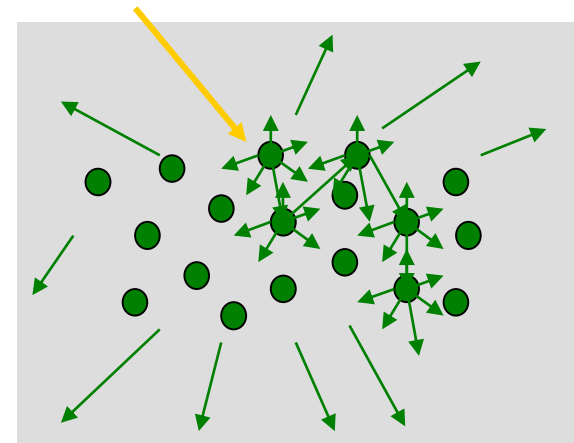
High size and/or concentration



## Scattering interface



**Scattering medium**  
(absorption and multiple scattering by particles)



## Mie theory



Sky

Rayleigh ( $r \ll \lambda$ )

Isotrope scattering in  $1/\lambda^4$

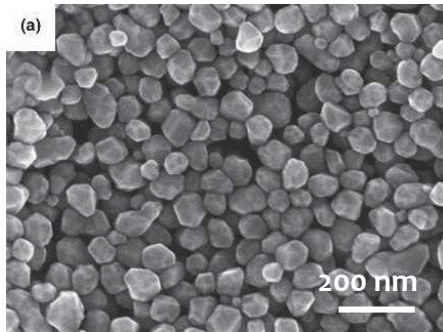
Cloud

Geometrical optics ( $r \gg \lambda$ )

Forward scattering independent of  $\lambda$

$\ll \lambda$  : nanometric scale

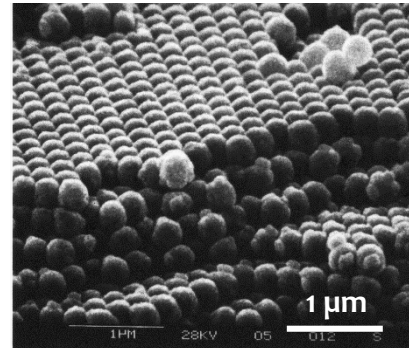
Homogeneous effective medium



Ag nanoparticles (80 nm) in solution

$\sim \lambda$  : hundreds of nanometers

Diffractive and interferential effects

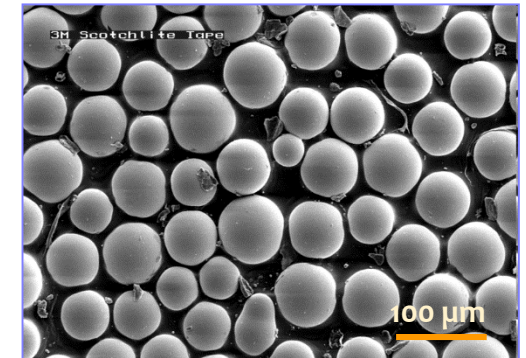


Opale

Arrangement of SiO<sub>2</sub> spheres (300 nm)

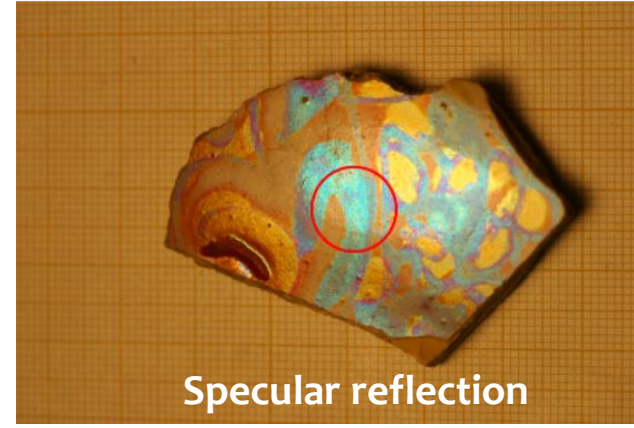
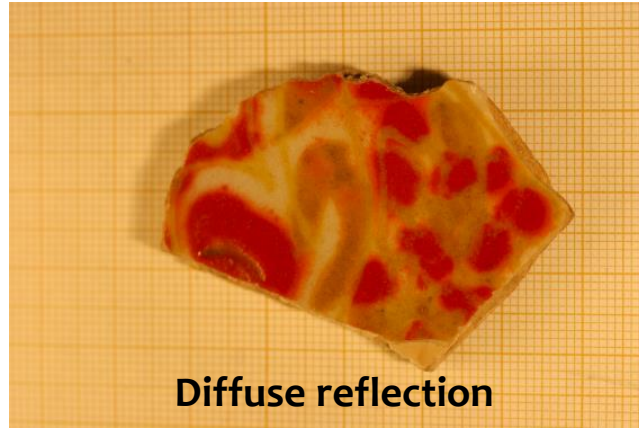
$\gg \lambda$  : micrometric scale

Optic geometric approach



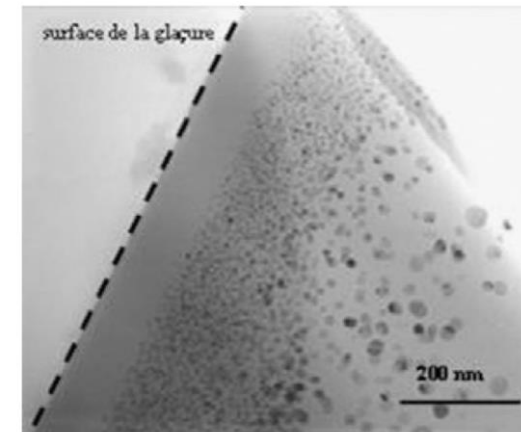
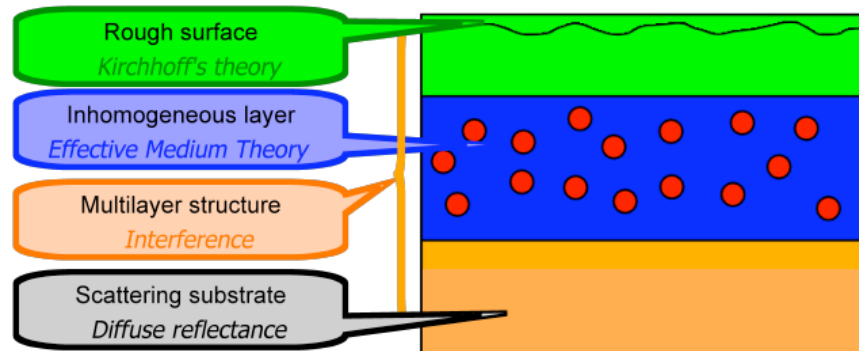
Retroreflective coating  
Microbeads (80 μm) of SiO<sub>2</sub>

## Enamels with metallic glaze

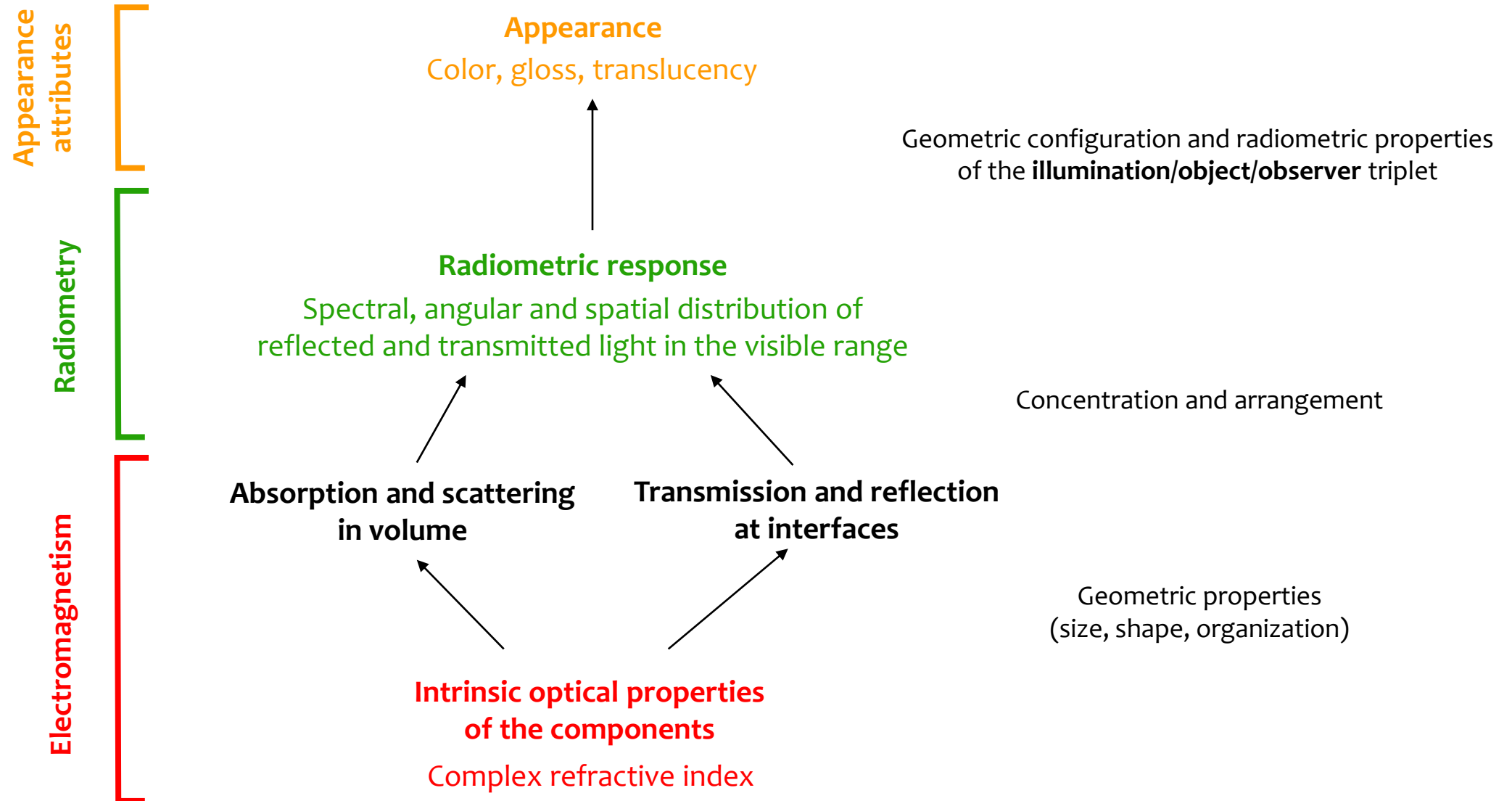


J. Lafait et al., Comptes Rendus Physique (2009)

### Locally → multilayer approach

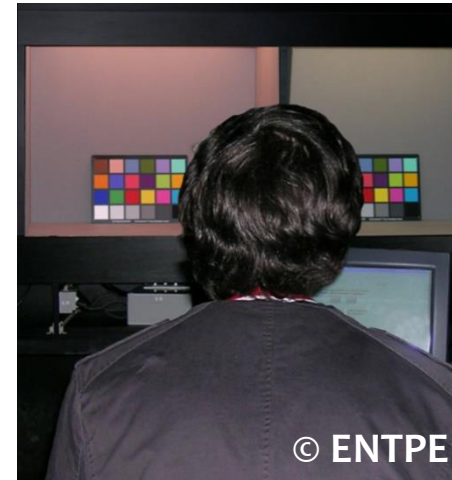




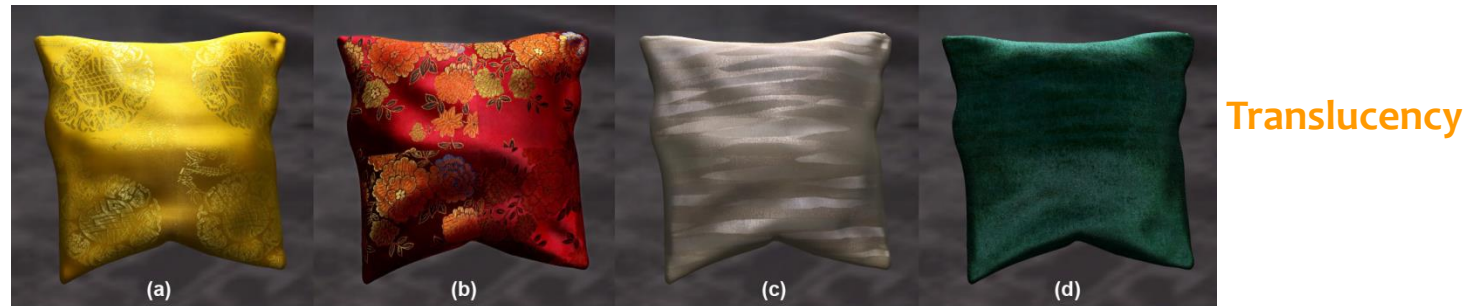


The spectral, angular and spatial variations of the scattered light  
can be linked to **the attributes of appearance**

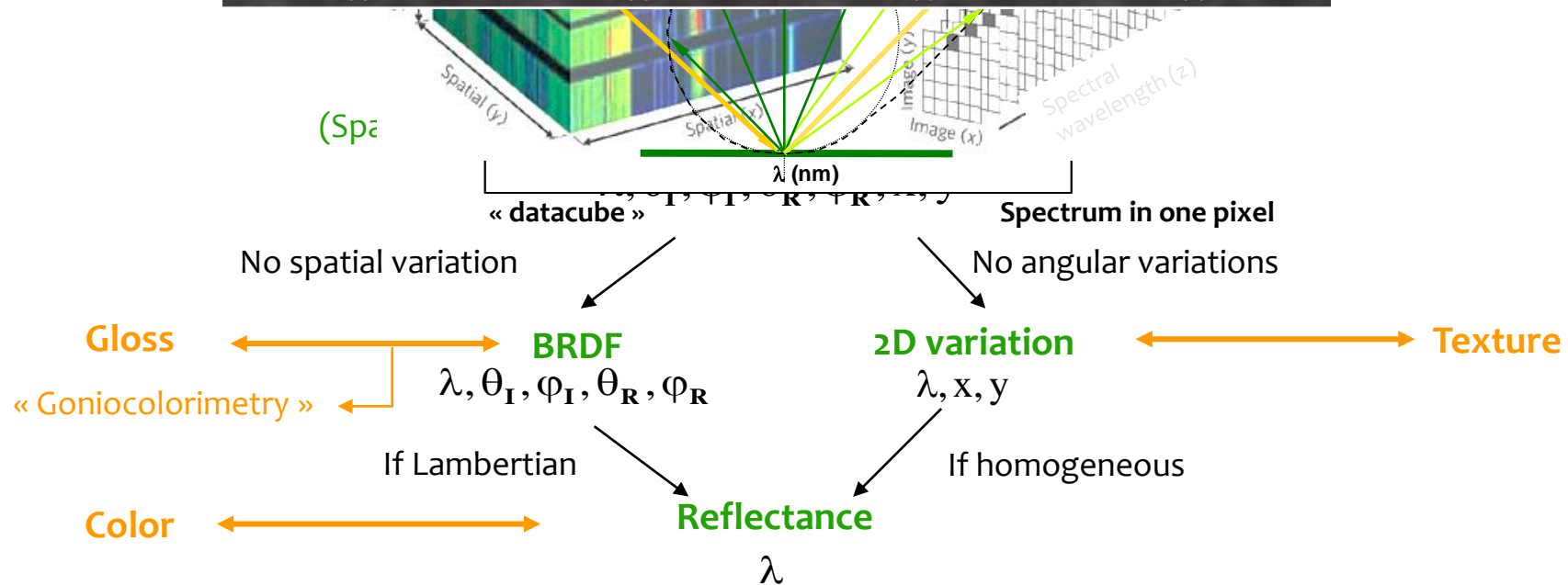
- Psycho-visual experiments
- Standardization by CIE for diffuse colors
- Much remains to be done for others appearance attributes



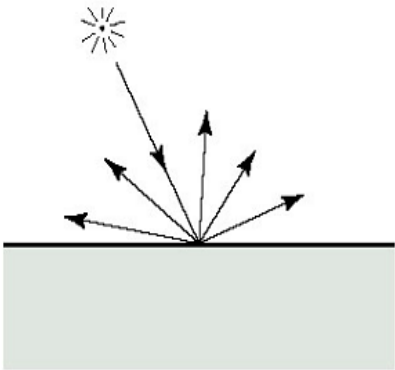
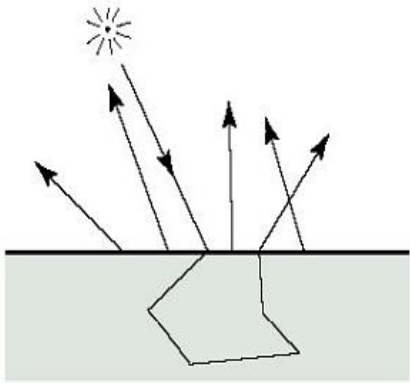
The spectral, angular and spatial variations of the scattered light  
 can be linked to **the attributes of appearance**



Translucency



**BSSRDF**



**BRDF**

## Radiometric response

Spectral, angular and spatial distribution of reflected and transmitted light in the visible range



**Direct problem**

## Parameters describing the object

Complex refractive indices of each component

Size, shape, concentration and organisation of the heterogeneities (surface and volume)

The more you want a complete description of the radiometric response, the more you need to know the material accurately  
→ a lot of strategies to simulate an average response

## Radiometric response

Spectral, angular and spatial distribution of reflected and transmitted light in the visible range



**Inverse problem**

→ Identify components

→ Quantify their concentrations, sizes, shapes

## Parameters describing the object

Complex refractive indices of each component

Size, shape, concentration and organisation of the heterogeneities (surface and volume)



James Turrell, *Afrum I (White)*, Guggenheim collection (1967)

## Variation of the perceived radiance

depending on whether the illumination light is collimated or diffuse



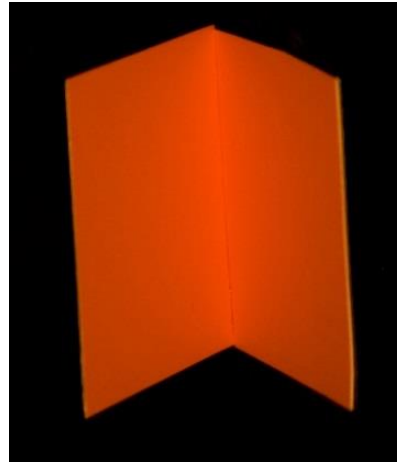
### Assumptions and parameters

Infinitely long V-cavity

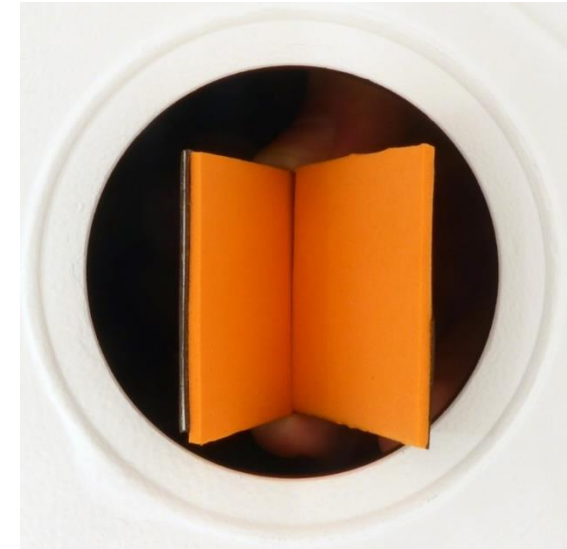
Lambertian material of reflectance  $\rho$

Aperture angle of the cavity  $\alpha$

## Interreflections in a diffuse V-cavity

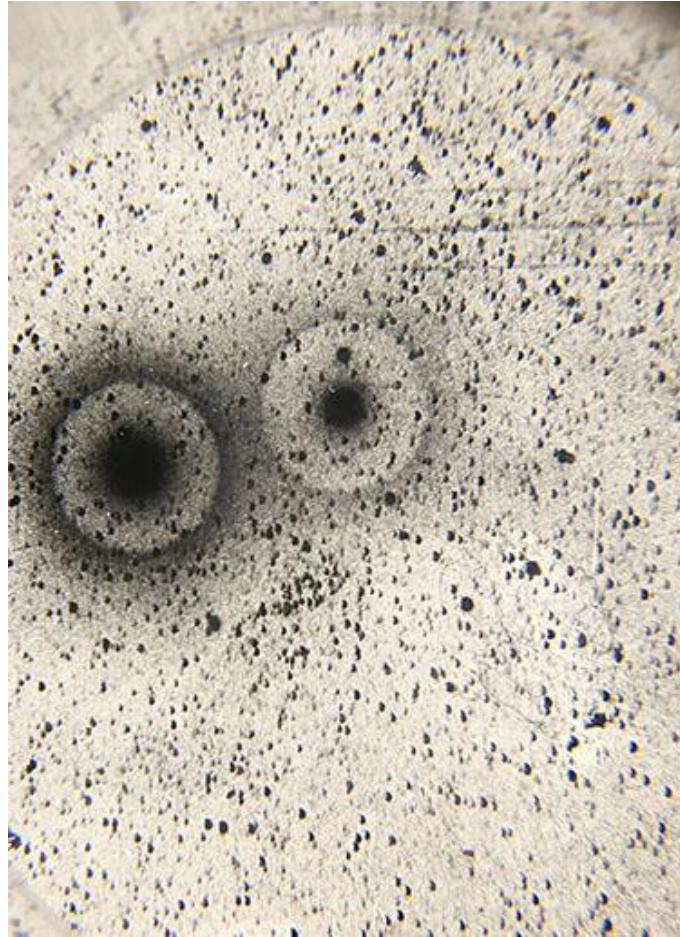


Frontal illumination



Diffuse illumination



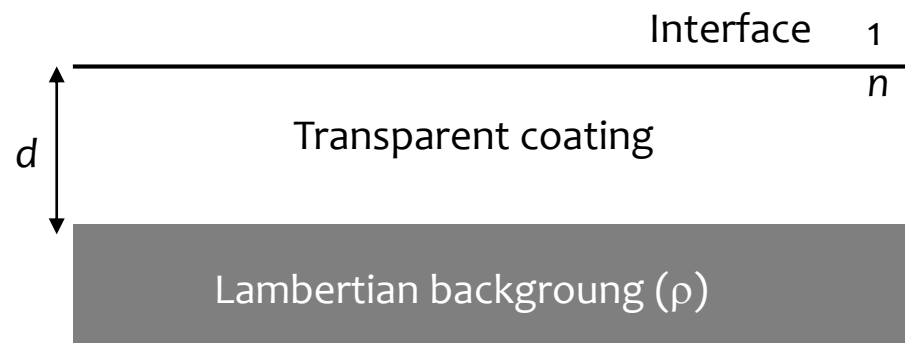


Photograph on glass plate of the Milky Way (in negative). E.E. Barnard, about 1892-1895  
© Lick observatory

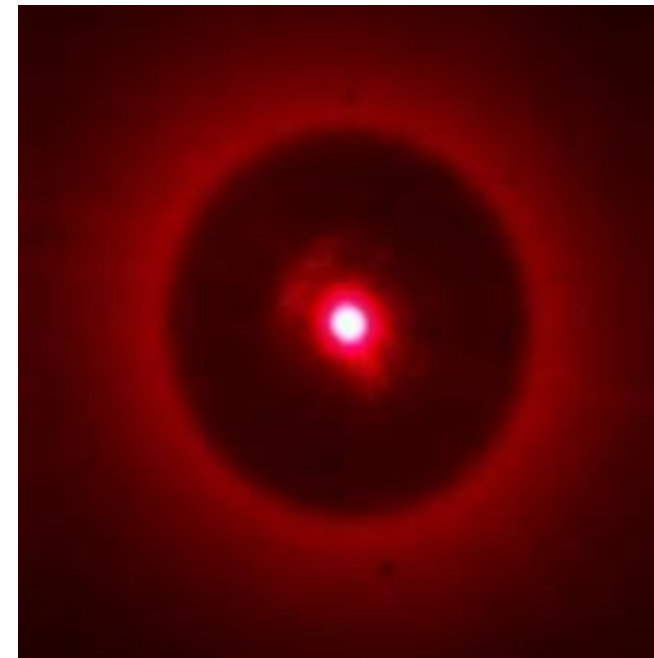
Global radiometric response



Assumptions and parameters



Halo in a transparent coating on a diffuse substrate

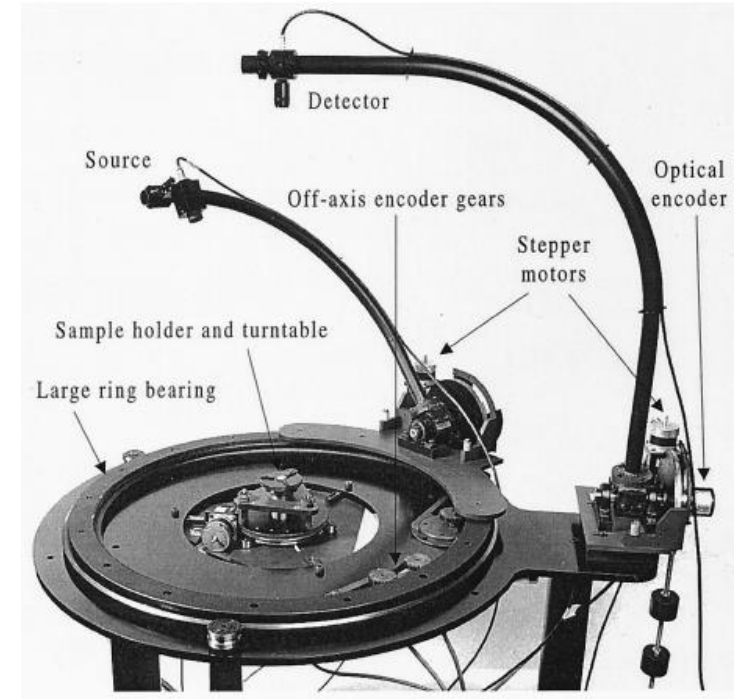


4 mm thick glass plate in optical contact with a paper, illuminated with a red laser diode © Morgane Gerardin

## Limitations related to radiometric measurement possibilities

- There are no standardized measurements of BSSRDF
- BRDF measurements have low signal-to-noise ratios especially at grazing angles and often poor angular resolution
- Even for spectral measurements, it is difficult to measure reflectances of translucent materials.

→ Need to collaborate with metrologists



D.R. White *et al.*, Applied Optics (1998)

## Error estimation between simulations and measurements

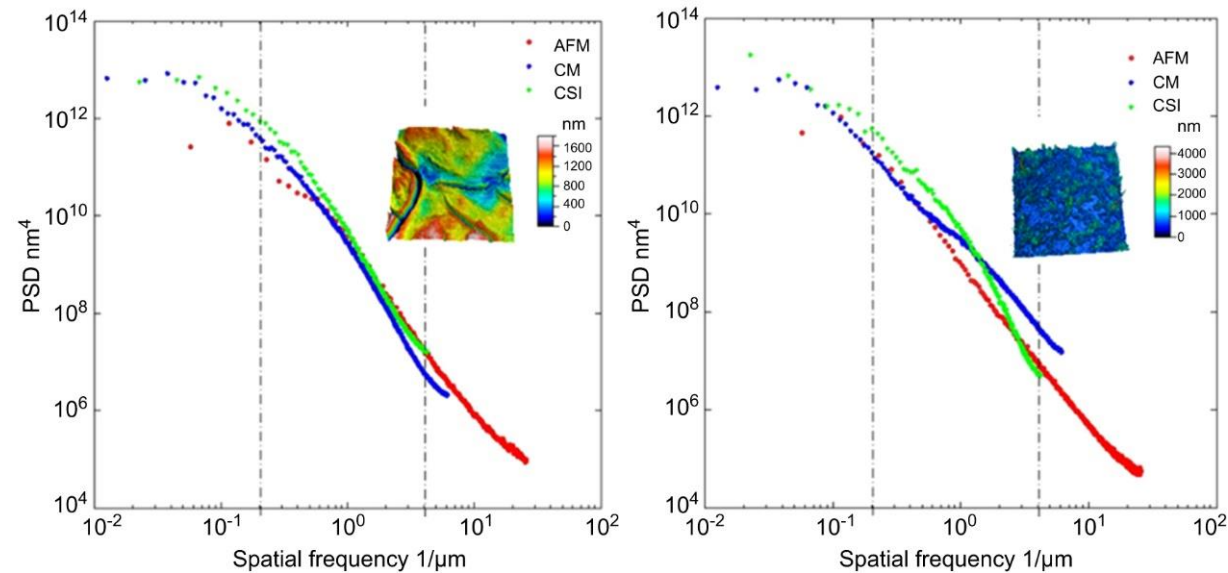
- rms error doesn't represent the difference in perception  $\rightarrow \Delta E$  in colorimetry
- Which error for BRDF? Which weight for the diffuse part and for the specular lobe?
- Sparse measured data: interpolation/extrapolation errors

**Know, measure or estimate the parameters describing the materials**

How to measure complex refractive indices for non-flat (rough surface, powder) or non-opaque materials?

## Know, measure or estimate the parameters describing the materials

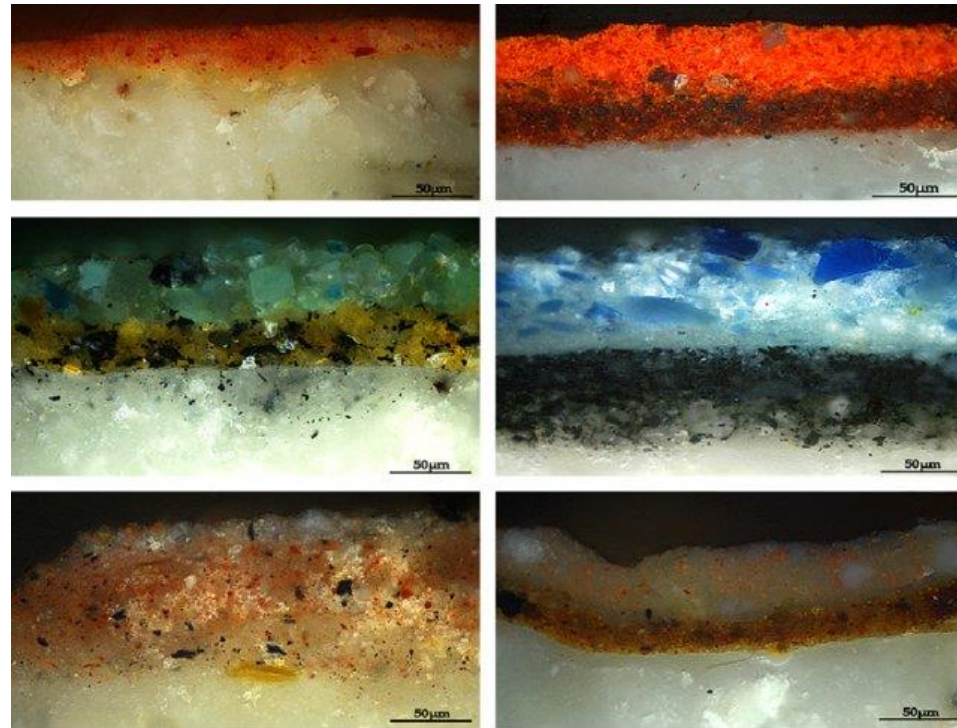
Measurement of surface topography: which spatial frequency range has an impact on the radiometric response?



Coherence scanning interferometer (CSI)  
Confocal microscope (CM)  
Atomic force microscope (AFM)

**Know, measure or estimate the parameters describing the materials**

How to have a correct evaluation of the size, shape and organisation of the particles?



**Cross-sections of several shades in the St Stephen wall paintings**  
S. Daniila, *Journal of Archaeological Science* (2008)

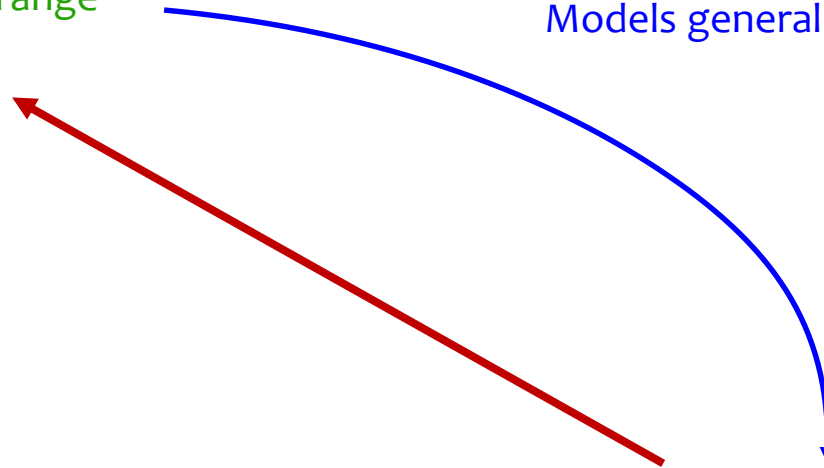
**Radiometric response**  
Spectral, angular and spatial distribution of reflected and transmitted light in the visible range

Model parameters cannot be measured independently.  
Models generally feed on themselves!

**Parameters describing the object**  
Complex refractive indices of each component  
Size, shape, concentration and organisation of the heterogeneities (surface and volume)



**Model parameters**  
Roughness parameter / slope distribution  
Absorption and scattering coefficients / phase function





**Radiometric approach is possible for ideal situations and a small number of parameters**

**Combined approach (radiometry and machine learning) could be efficient for more complex systems**

**Appearance prediction models should be adapted to measurements facilities**